

# Law of Motion

# LAW OF MOTION

Velocity

$$LT^{-1}$$

m/sec

accel<sup>n</sup>

$$LT^{-2}$$

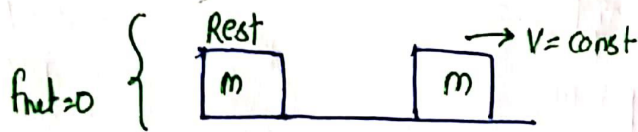
m/sec<sup>2</sup>

dir<sup>n</sup> - Motion ke along

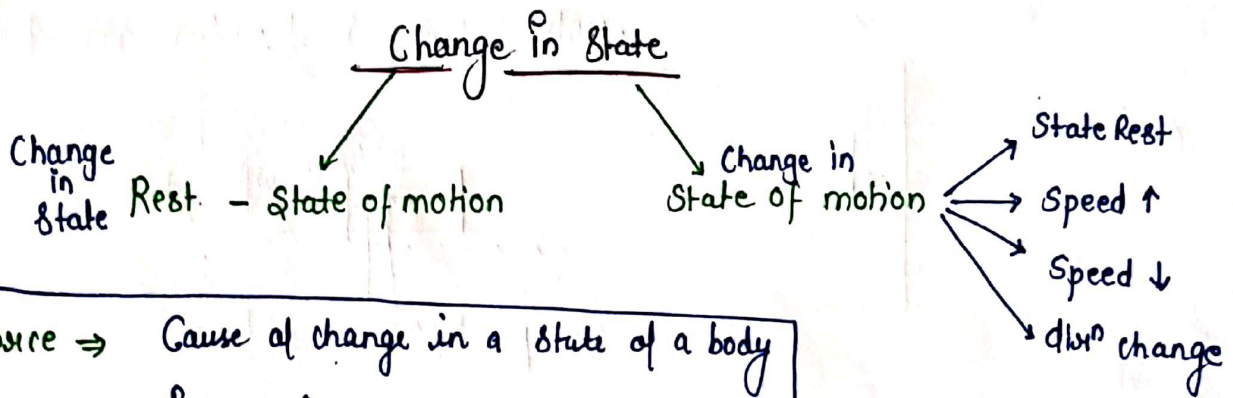
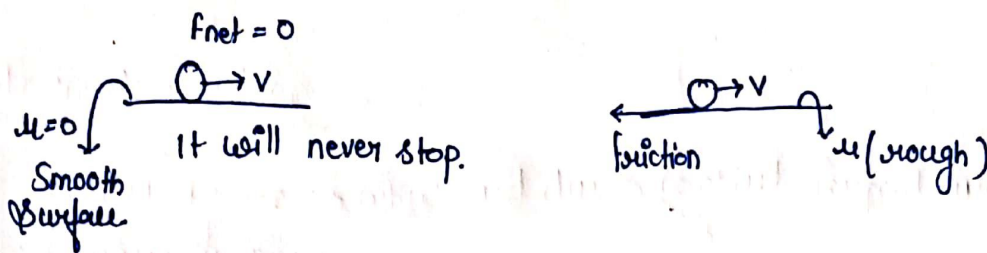
accel<sup>n</sup> - Force ke along or change in velocity.

Physical state of a body define with the help of Velocity.

1. State of Rest
2. State of Uniform motion ( $V = \text{const}$ )
3. No net force required to keep the object in a same state



Ex!



INERTIA  $\Rightarrow$  Property of a body due to which it oppose the cause of change in state of a body

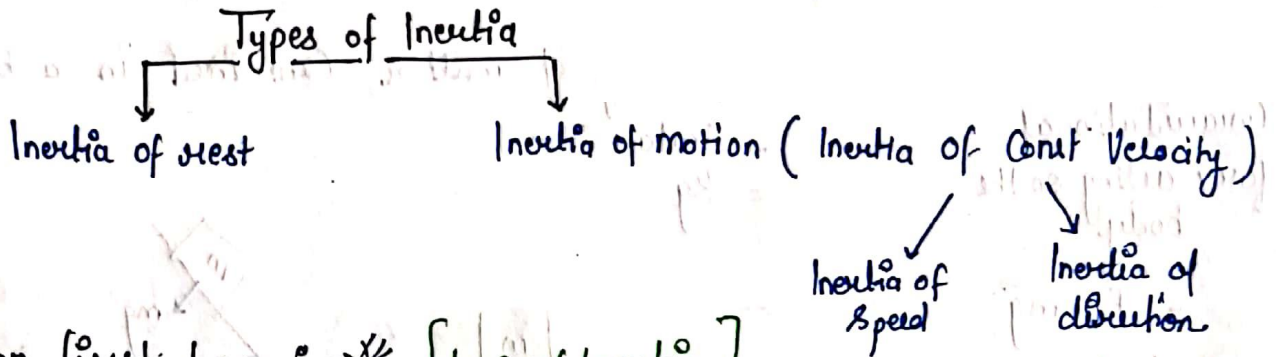
Inertia oppose motion = false

Inertia oppose cause of change in Motion  $\rightarrow$  True

- ⇒ Inertia is not a physical quantity.
- ⇒ Unit & dimension less
- ⇒ It cannot be measured but it can be compared

**Inertia & mass**

↳ Can be compared, but can't be measured.



Newton's first law :  $\Rightarrow$  [Law of Inertia]

IF  $(F_{ext})_{Net} = 0$  then state of a body remains same

equilibrium.  $\vec{v} = \text{const} / \vec{v} = 0$   
hence  $\vec{a} = 0$

Ques when an object is in equilibrium state, then

1. It must be at rest
2. No force is acting on it
3. Its net acceleration must be zero
4. All of these

Ans when an object is at rest.

- ① force is required to keep it in rest state
- ② No force is acting on it.
- ③ A large number of forces may be acting on it which balance each other
- ④ It is in vacuum.

Ques An athlete does not come to rest immediately after crossing the winning line due to the

- ① Inertia of rest
- ② Inertia of motion
- ③ Inertia of direction
- ④ None

Ans

Ques If a force of constant magnitude acts in direction perpendicular to the motion of a particle, then its.

1. Speed is Uniform ✓
2. Momentum is Uniform
3. Velocity is Uniform
4. All of these

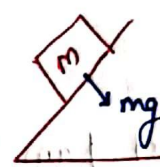
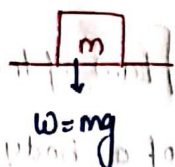
Weight  $\Rightarrow$  Gravitational force acting on the body.

Mass  $\Rightarrow$  quantity of matter contained in a body.

$=$  Scalar  
 $=$  Kg

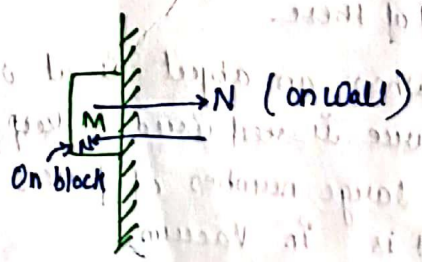
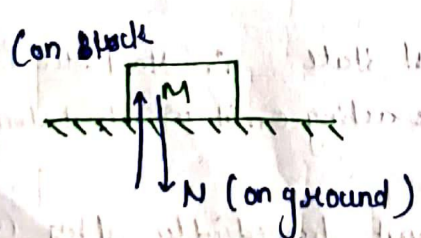
$= \vec{F} = m\vec{g}$

- $=$  Vector
- $=$  Newton
- $=$  direction always towards centre of earth (downwards)

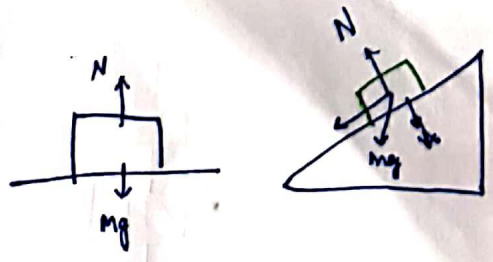


Normal Reaction  $\Rightarrow$

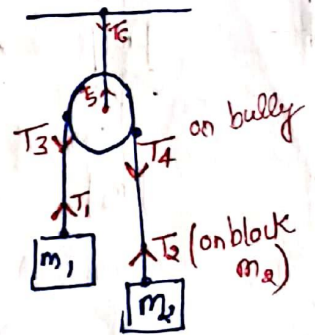
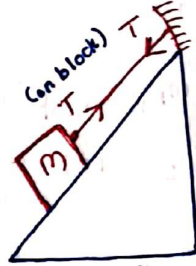
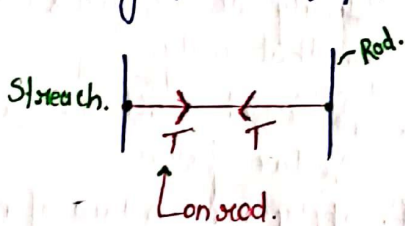
- # Contact force  $\Rightarrow$  which act due to contact, perpendicular to the contact
- # Always in pair - equal and opposite
- # perpendicular to contact surface



Normal Reaction  $\Rightarrow$



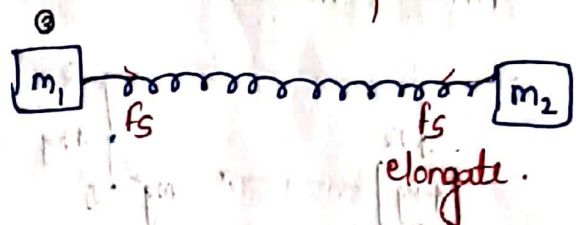
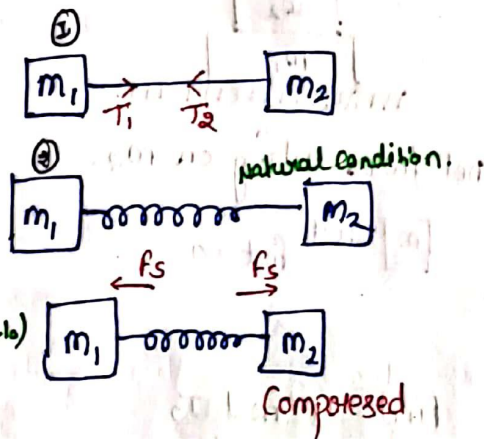
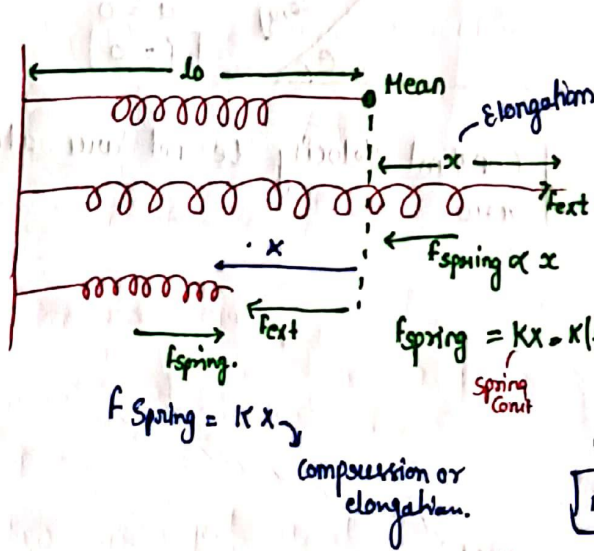
Tension force  $\Rightarrow$  H away from contact point along the length of string  
 = In ideal string (Massless), Tension same at all the point



$$T_1 = T_2 = T_3 = T_4$$

ideal string = value same

Spring  $\Rightarrow$  Force always towards the mean position.



Newton first law of motion  $\Rightarrow$

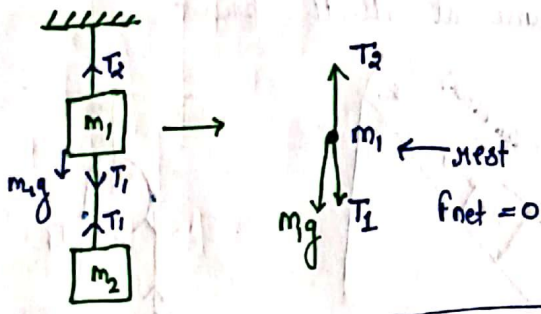
= Law of Inertia / Law of equilibrium  
 = qualitative definition of motion

$$\text{If } \sum F_{net} = 0 \text{ then } \sum a_{sys} = 0 \text{ hence } \vec{v} = \text{const}, \vec{a} = 0$$

If net force acting on body is zero then it will continuous its state.

$$\frac{\sum F_x = 0 \text{ then } \vec{a}_x = 0 \quad \text{y का-ही पता}}{\sum F_y = 0 \text{ then } \vec{a}_y = 0 \quad \text{x का-ही पता}}$$

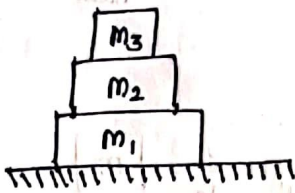
F.B.D  $\Rightarrow$  free body diagram  $\rightarrow$



$$T_2 = T_1 + m_1g$$

1. Take that body separate from the system & represent it by point.
2. Identify all the forces acting on that body.
3. Represent all the forces in vector form.
4. apply newton law of motion.

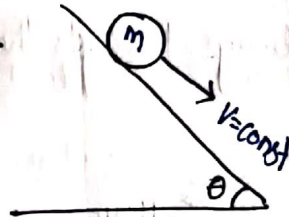
Ques



net force acting on  $m_2$ .

$$m_2 \text{ rest } f_{net} = 0$$

Ques



And net force on

$$m = ?$$

$$\vec{v} = \text{const}$$

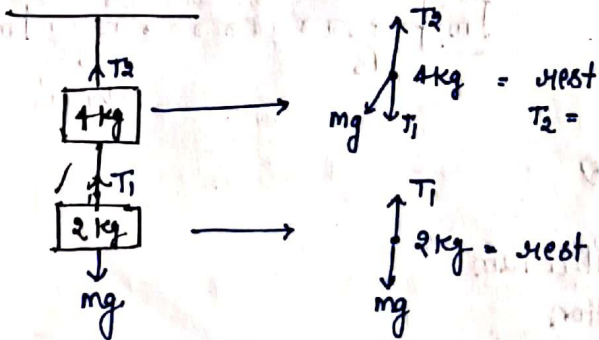
$$a = 0$$

$$f = 0$$

Constant Velocity  $\Rightarrow$  net force always zero

Ques

Find  $T_1$  and  $T_2$



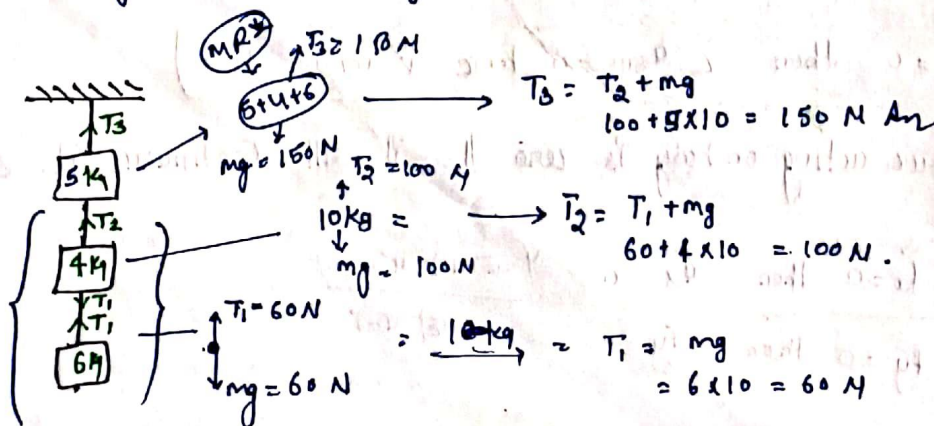
$$4\text{kg} = \text{rest}$$

$$T_2 = T_1 + mg = 20 + 4 \times 10 = 60 \text{ N Ans}$$

$$2\text{kg} = \text{rest}$$

$$\begin{cases} T_1 = mg \\ T_1 = 2 \times 10 = 20 \text{ N} \end{cases}$$

Ques



$$T_3 = T_2 + mg$$

$$100 + 5 \times 10 = 150 \text{ N Ans}$$

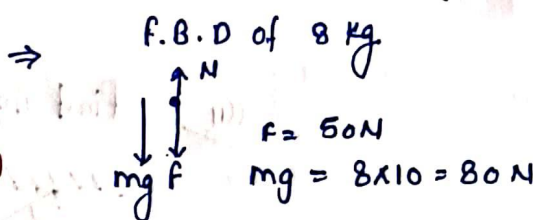
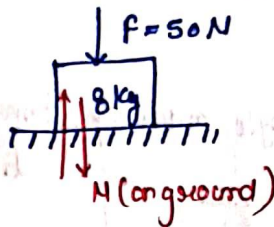
$$T_2 = T_1 + mg$$

$$60 + 4 \times 10 = 100 \text{ N}$$

$$T_1 = mg$$

$$= 6 \times 10 = 60 \text{ N}$$

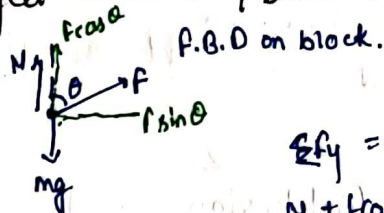
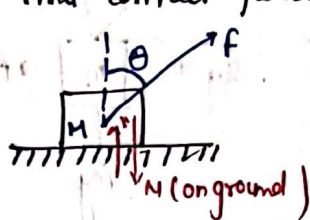
Q1 Find contact force (Normal) b/w 8 kg and ground.



$$N = 50 + 80$$

$$N = 130 \text{ N}$$

Q2 Find contact force on object towards by block??

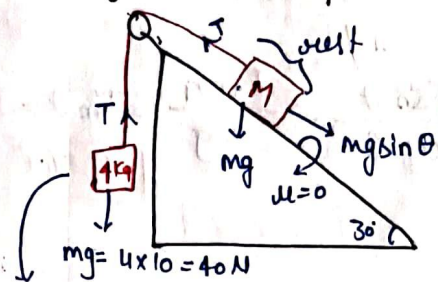


$$\sum F_y = 0$$

$$N + F \cos \theta = mg$$

$$N = (mg - F \cos \theta) \quad \underline{\underline{\text{Ans}}}$$

Q3 If system is in equilibrium then find value of (m)



$$T = mg \sin \theta \quad \text{--- (1)}$$

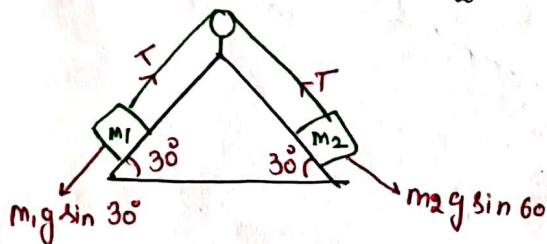
$$4g = m \times 10 \times \sin 30^\circ$$

$$4 = m \times \frac{1}{2}$$

$$m = 8 \text{ Kg}$$

$$T = 40 \text{ N} \quad \text{--- (2)}$$

Q4 Find relation b/w  $m_1$  &  $m_2$  so that system is in equilibrium.

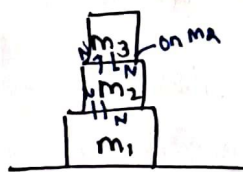


$$m_1 g \sin 30 = m_2 g \sin 60$$

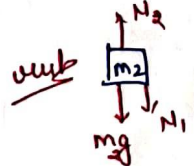
$$m_1 \left(\frac{1}{2}\right) = m_2 \times \frac{\sqrt{3}}{2}$$

$$m_1 = \sqrt{3} m_2 \quad \underline{\underline{\text{Ans}}}$$

Q5 Find force applied by  $m_1$  on  $m_2$



F.B.D of  $m_2$

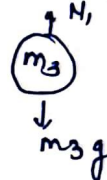


$$N_2 = N_1 + m_2 g$$

$$N_2 = m_3 g + m_2 g$$

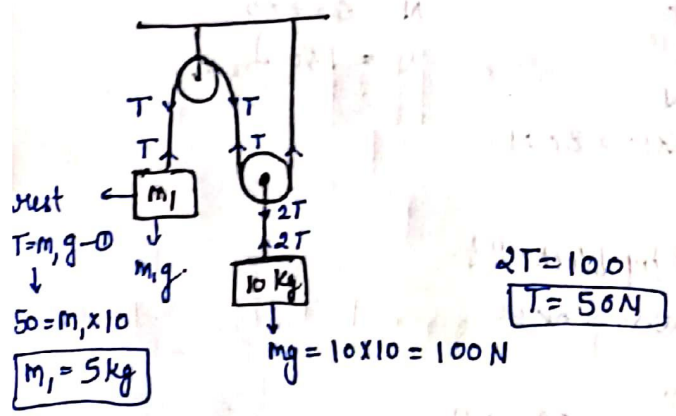
$$N_2 = g(m_3 + m_2) \quad \underline{\underline{\text{Ans}}}$$

F.B.D of  $m_3$



$$N_1 = m_3 g$$

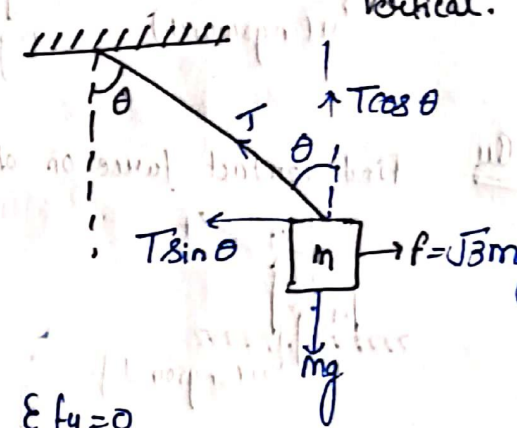
Q1 Find  $m$  so that system is in equilibrium



And find tension

$(i)^2 + (ii)^2$   
 $T^2 (\sin^2 \theta + \cos^2 \theta) = (mg)^2 + (3mg)^2$   
 $T^2 = 4m^2g^2$   
 $T = \sqrt{4m^2g^2}$   
 $T = 2mg$

Q2 Find Angle made by string from Vertical.



$\Sigma f_y = 0$   
 $T \cos \theta = mg$  — (i)  
 $T \sin \theta = \sqrt{3}mg$  — (ii)

$\frac{T \sin \theta}{T \cos \theta} = \frac{\sqrt{3}mg}{mg}$   
 $\tan \theta = \sqrt{3}$   
 $\theta = 60^\circ$

Q3 The Tension (T) in the string (assumed to be weightless) in the arrangement shown is (neglect friction everywhere) if system is in equilibrium.

- ① 50 N
- ② 25 N
- ③ 30 N
- ④ 500 N



Q. A vertical force  $F$  is applied at one end of a uniform rope of mass  $M$  and length  $L$ . Find out tension in the rope as a function of  $x$ .

- ①  $F + mg$
- ②  $F + \frac{mgL}{x}$
- ③  $\frac{FL + Mg x}{L}$  ✓
- ④  $\frac{Fx + MgL}{L}$

Q. Find normal reaction (Contact force) b/w A & B.

The diagram shows three blocks stacked vertically on a surface. Block A is at the bottom with a mass of 6 kg. Block B is in the middle with a mass of 2 kg. Block C is at the top with a mass of 4 kg. Normal reaction forces are labeled as  $N_1$  (between C and B),  $N_2$  (between B and A), and  $N_3$  (between A and the ground).

**F.B.D of 'C'**

$\sum f_y = 0$   
 $N_1 = 40\text{ N}$   
 $mg = 40\text{ N}$

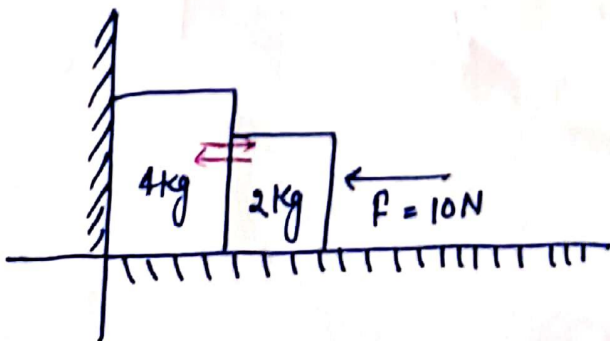
**F.B.D of 'B'**

$\sum f_y = 0$   
 $N_2 = N_1 + mg$   
 $N_2 = 40 + 20 = 60\text{ N}$   
 $mg = 20\text{ N}$

**F.B.D of 'A'**

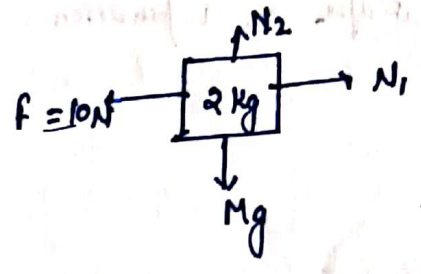
$\sum f_y = 0$   
 $N_3 = N_2 + mg$   
 $= 60 + 60$   
 $N_3 = 120\text{ N}$   
 $mg$

Find Contact force b/w 4kg and 2kg.



$\sum f_x = 0$   
 $N_1 = 10\text{ N}$

F.B.D of '2 kg'



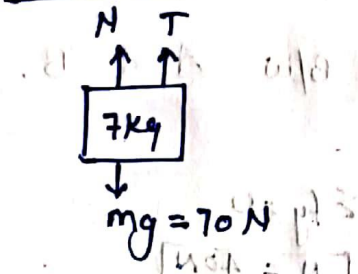
$$N_2 = Mg$$

$$N_2 = 20 N$$

$$\sum f_y = 0$$

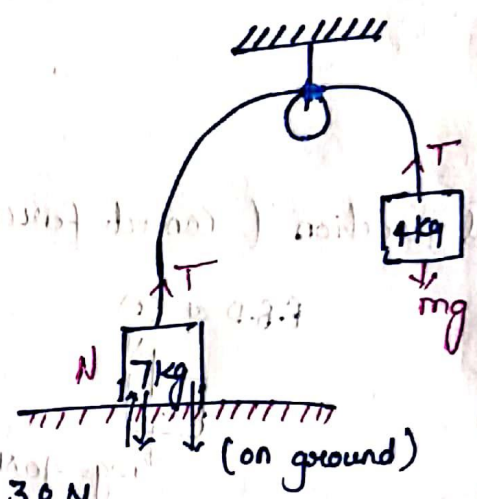
Find Contact force b/w ground 7 kg Block

F.B.D



$$T + N = 70$$

$$N = 70 - 7 = 70 - 40 = 30 N$$



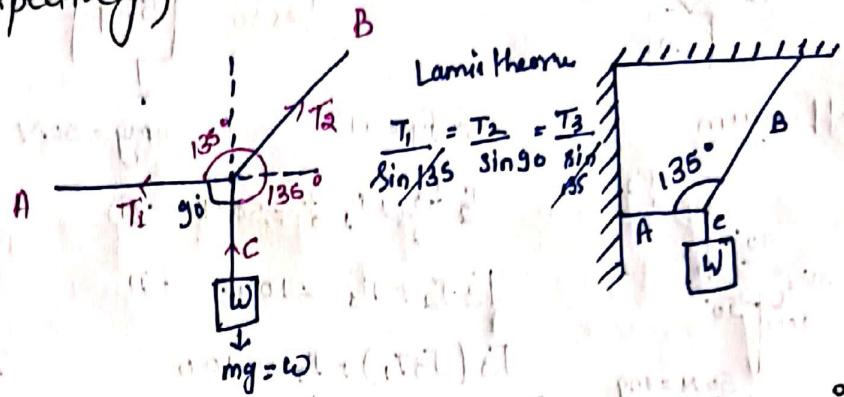
rest

$$T = mg = 40 N$$

Que A Uniform rope of mass  $M$  and Length  $L$  is fixed at its upper end vertically from a rigid support, then the tension in the rope at the distance  $l$  from the rigid support is

Ques A block of weight  $W$  is supported by three strings as shown in figure which of the following relation is true for tension in the strings? (Here  $T_1$ ,  $T_2$  and  $T_3$ ) are the tension in the string A, B and C respectively.)

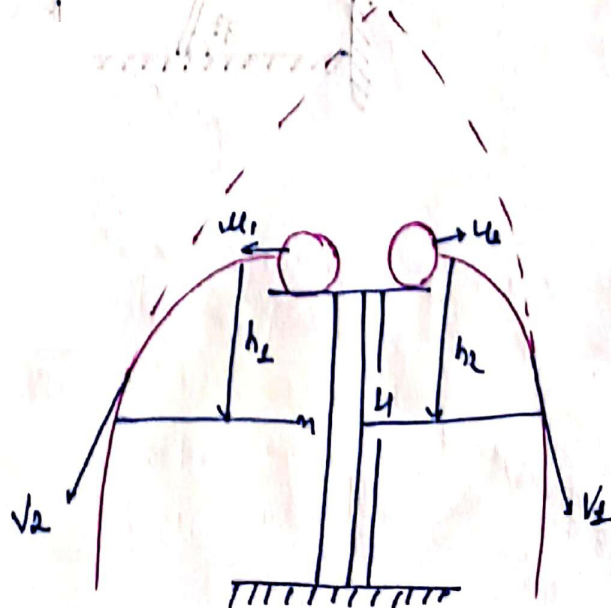
1.  $T_1 = T_2$
2.  $T_1 = T_3$  ✓
3.  $T_2 = T_3$
4.  $T_1 = T_2 = T_3$

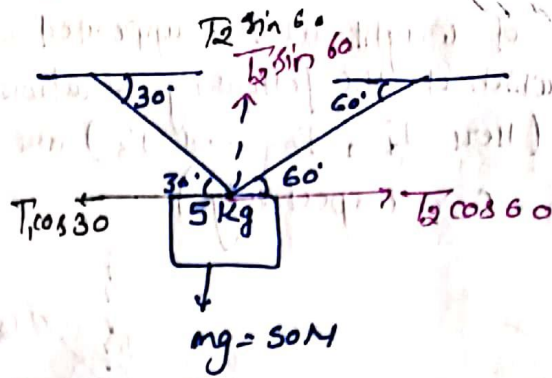
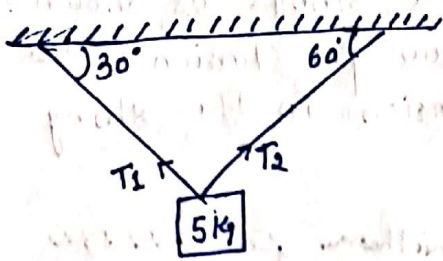


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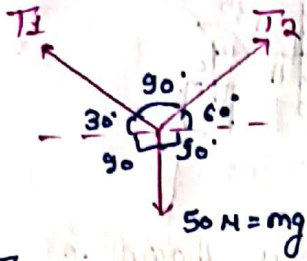
- ①  $T_1 = T_2$
- ②  $T_1 = T_3$
- ③  $T_2 = T_3$
- ④  $T_1 = T_2 = T_3$

Ques Find time when they are moving I/r to each other also find sep<sup>n</sup> B/w them when they are I/r to each other





Lami's theorem



$$\sum F_y = 0$$

$$T_2 \frac{\sqrt{3}}{2} + T_1 \frac{1}{2} = 50 \text{ N} \quad \text{--- (1)}$$

$$\sqrt{3} T_2 + T_1 = 100 \quad \text{--- (2)}$$

$$\sqrt{3} (\sqrt{3} T_1) + T_1 = 100$$

$$4 T_1 = 100$$

$$T_1 = 25 \text{ N}$$

$$\sum F_x = 0$$

$$T_1 \frac{\sqrt{3}}{2} = T_2 \frac{1}{2}$$

$$\sqrt{3} T_1 = T_2 \quad \text{--- (3)}$$

$$T_2 = 25 \sqrt{3} \text{ N}$$

$$\frac{T_1}{\sin 150} = \frac{50}{\sin 90}$$

$$T_1 = 50 \times \frac{1}{2} = 25 \text{ N}$$

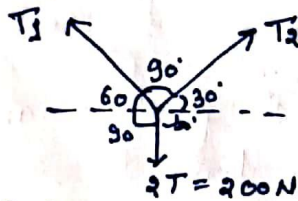
Q4 In the arrangement as shown, tension  $T_2$  is ( $g = 10 \text{ m/s}^2$ )

① 50 N

② 100 N

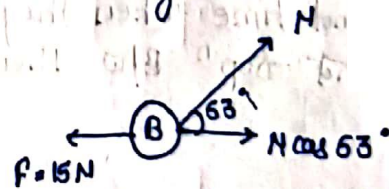
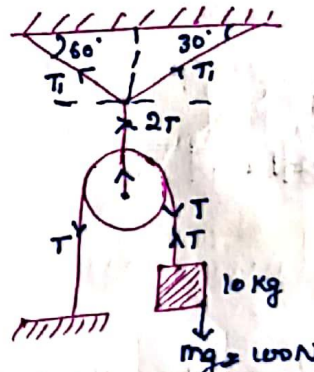
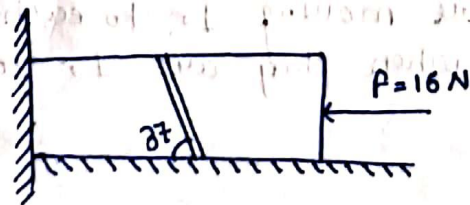
③  $50\sqrt{3}$  N

④  $100\sqrt{3}$  N



$$\frac{T_2}{\sin 150} = \frac{200}{\sin 90} = T_2 = 200 \times \frac{1}{2} = 100 \text{ N}$$

Q5 find Contact force between them.



$$\sum F_x = 0$$

$$16 = N \times \frac{3}{5}$$

$$N = 25 \text{ N}$$

Ques find  $f$  so that object of mass  $m$  will at rest as shown in figure

$$T = F + F \cos \theta$$

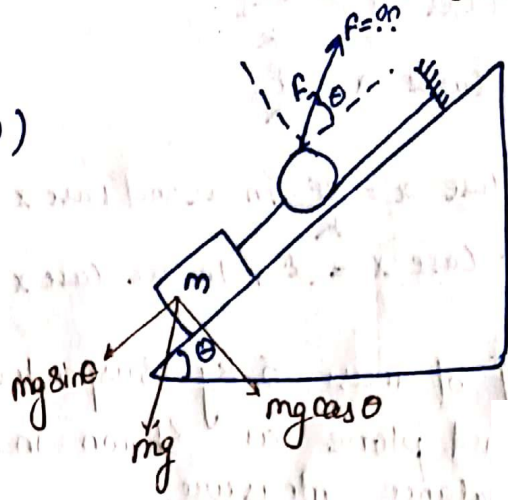
$$mg \sin \theta = f(1 + \cos \theta)$$

$$f = \frac{mg \sin \theta}{(1 + \cos \theta)}$$

$$f = \frac{mg \cdot \frac{\sin \frac{\theta}{2} \cos \frac{\theta}{2}}{\cos \frac{\theta}{2} \cos \frac{\theta}{2}}}{\frac{\cos \frac{\theta}{2} \cos \frac{\theta}{2}}{\cos \frac{\theta}{2} \cos \frac{\theta}{2}}}$$

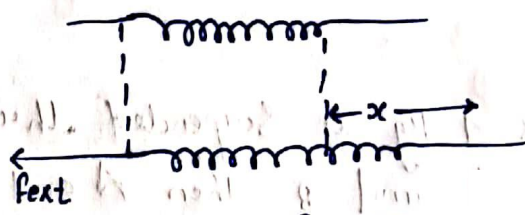
$$f = mg \tan \left( \frac{\theta}{2} \right)$$

Ans



Ideal - Spring (Massless)

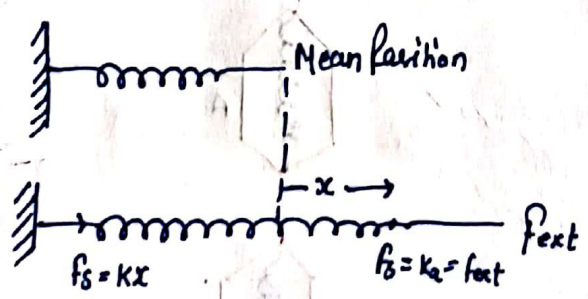
$N=0$   
Body Contact Remove



$$F_s = kx$$

$$\{ F_s = F_{ext} \}$$

String assume



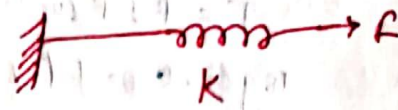
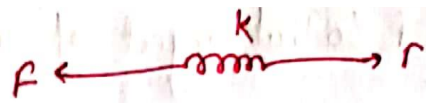
Ques figure shows two cases. In first case a spring (spring constant  $k$ ) is pulled by two equal and opposite forces at both ends in second case is pulled by a force  $f$  at one end. Extension ( $x$ ) in the spring will be.

① In both cases  $x = \frac{2F}{k}$

② In both cases  $x = \frac{F}{k}$

③ In first case  $x = \frac{2F}{k}$  in second case  $x = \frac{F}{k}$

④ In first case  $x = \frac{F}{k}$ , In sec case  $x = \frac{2F}{k}$



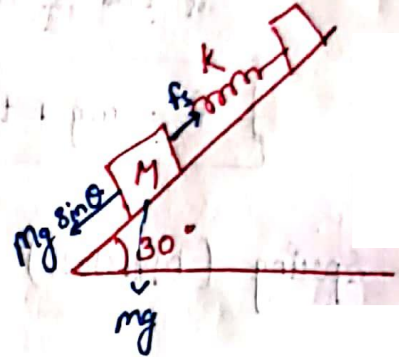
Ques A body of mass 5 kg suspended by a spring balance on an inclined plane as shown in figure. The spring balance measure

- ① 50 N
- ② 25 N ✓
- ③ 500 N
- ④ 10 N

$$F_s = mg \sin \theta$$

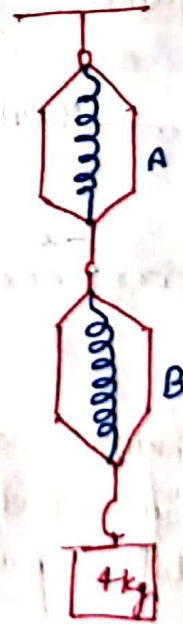
$$F_s = 5 \times 10 \times \sin 30^\circ$$

$$= 25 \text{ N} \quad \underline{\underline{\text{Ans}}}$$



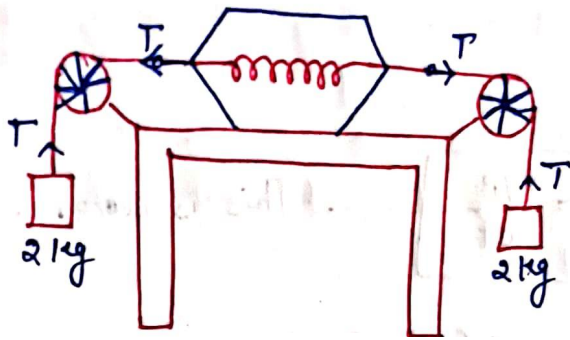
Ques A block of mass 4 kg is suspended through two light spring balance A and B. Then A and B will read respectively

- ① 4 kg and zero kg
- ② zero kg and 4 kg
- ③ 4 kg and 4 kg ✓
- ④ 2 kg and 2 kg

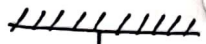


Ques As shown in figure, two equal masses each of 2 kg are suspended from a spring balance, the reading of the spring of the spring balance will be

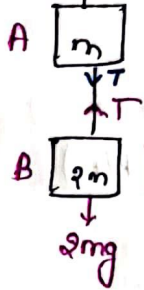
- ① zero ✓
- ② 2 kg
- ③ 4 kg
- ④ Between zero and 2 kg



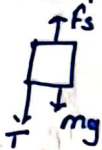
Ques



System as shown in figure is in equilibrium. If string is cut then find accel<sup>n</sup> of A & B



F.B.D of A

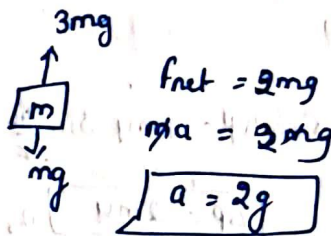
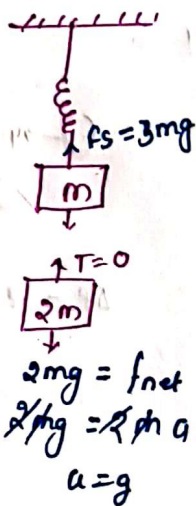


$$f_s = T + mg$$

$$= 2mg + mg = 3mg \quad \text{--- (i)}$$

$$T = 2mg \quad \text{--- (ii)}$$

after cutting



$$a = 2g$$

Momentum  $\Rightarrow$

Motion Contained in a body

$$P \propto v$$

$$P \propto M$$

$$P = m\vec{v}$$

= Vector, direction parallel to velocity

= Unit = kg m/sec.

Force

$$\vec{F}_{avg} = \frac{\Delta \vec{P}}{\Delta t}$$

$$\vec{F}_{inst} = \frac{dP}{dt}$$

This is Newton's 2nd Law.

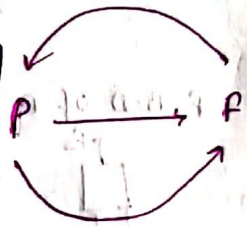
$$\vec{F}_{avg} = \frac{m[v_f - v_i]}{\Delta T}$$

= Slope of (P-t) is force  
= Vector physical quantity.  
= N

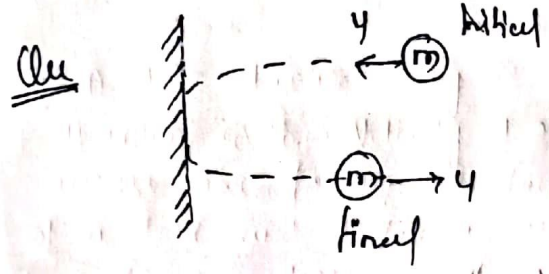
$$\vec{F}_{avg} = \frac{\int f dt}{\int dt}$$

$$\int f dt = \int dP \quad \Delta P = \int f dt = \text{area of } f-t$$

$$\Delta P = \int f \cdot dt$$



$$\frac{dP}{dt} = f = \text{slope of } (P/t)$$



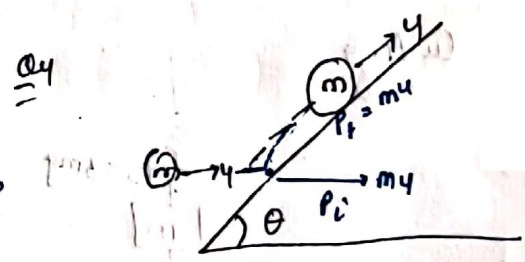
$\Delta P = 0$  OR  $\Delta P = 2mu \sin \frac{\theta}{2}$

$$\Delta P = \vec{P}_f - \vec{P}_i$$

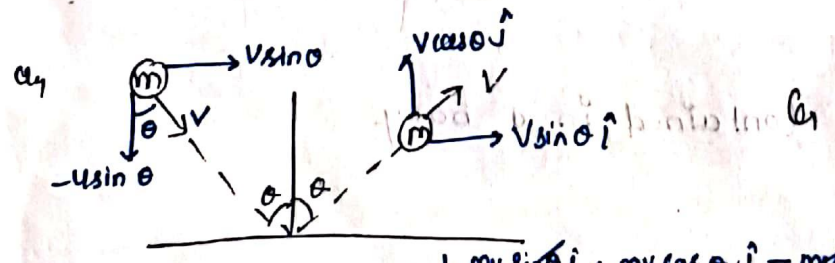
$$mu \hat{i} - (-mu \hat{i})$$

$$\Delta P = 2mu \hat{i}$$

$$|\Delta \vec{P}| = 2mu$$



$$\Delta P = 2mu \sin \left( \frac{\theta}{2} \right)$$

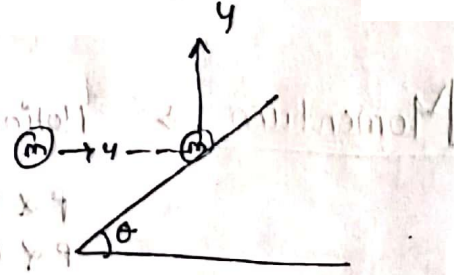


$$\vec{u}_i = v \sin \theta \hat{i} - v \cos \theta \hat{j}$$

$$\vec{v}_f = v \sin \theta \hat{i} + v \cos \theta \hat{j}$$

$$\Delta \vec{P} = \vec{P}_f - \vec{P}_i$$

$$\Delta P = 2mv \cos \theta \hat{j}$$



$$\Delta P = \vec{P}_f - \vec{P}_i$$

$$= mu \hat{j} - mu \hat{i}$$

$$\Delta P = \sqrt{(mu)^2 + (mu)^2}$$

$$= \sqrt{2m^2 u^2} \Rightarrow (\sqrt{2})mu$$



Newton 2<sup>nd</sup> Law  $\Rightarrow$

$$\vec{F}_{avg} = \frac{\vec{p}_f - \vec{p}_i}{\Delta t}$$

$$F_{avg} = \frac{\int \vec{f} \cdot dt}{\int dt}$$

$$F_{inst} = \frac{d\vec{p}}{dt}$$

The rate of change in momentum  
- force = Slope of p/t graph

$$\vec{F} = \frac{d(mv)}{dt}$$

$$F = m\vec{a} + v \frac{dm}{dt}$$

Newton 2<sup>nd</sup> Law

If  $m = \text{const}$

$$\vec{F} = m\vec{a}$$

$\vec{u} = \text{const}$  (m-variable)

$$f = v \left( \frac{dm}{dt} \right)$$

Ex:

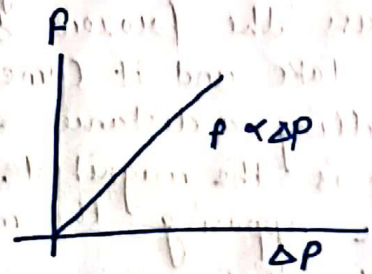
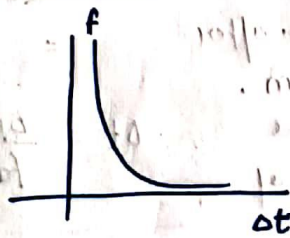
Stone

Cotton

$$F = \frac{p_f - p_i}{\Delta t}$$

$$F \propto \frac{1}{\Delta t}$$

Graph



Que

A Cricketer catches a ball of mass 150g in 0.1s moving with speed 20m/s, then the experience force of.

- ① 300 N
- ② 30 N ✓
- ③ 8 N
- ④ 0.3 N

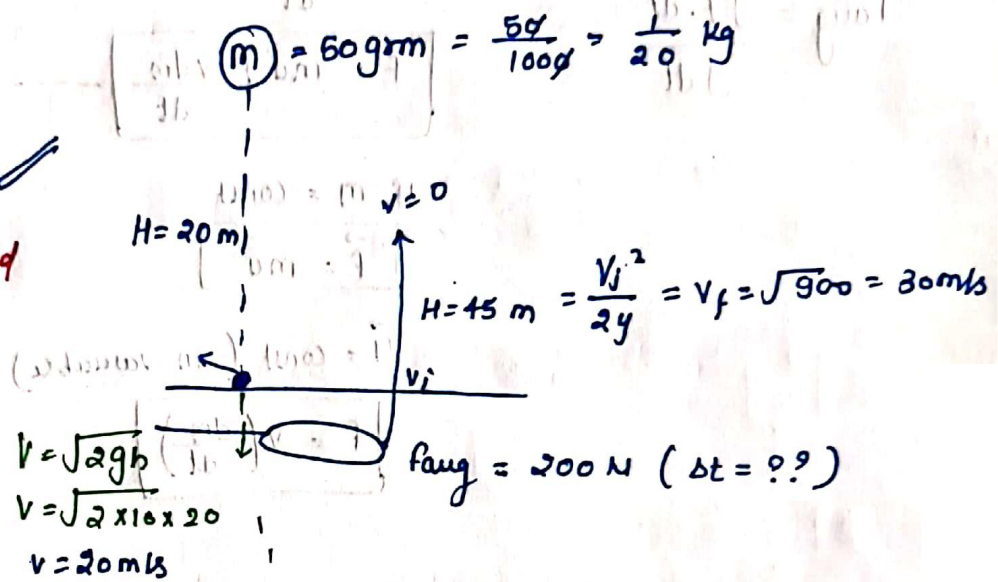
$$m \rightarrow v = 20 \text{ m/s}$$

$$p_i = mv = \frac{150}{1000} \times 20 = 3$$

$$\frac{\Delta p}{\Delta t} = \frac{3}{\frac{1}{10}} = 30 \text{ N } \underline{\underline{\text{Ans}}}$$

Q A ball of mass 50g is dropped from a height of 20 m. A boy on the ground hits the ball vertically upward with a bat with an average force of 200 N, so that it attains a vertical height of 45 m. The time for which the ball remains in contact with the bat is (Take  $g = 10 \text{ m/s}^2$ )

- ①  $\frac{1}{20}^{\text{th}}$  of a second
- ②  $\frac{1}{40}^{\text{th}}$  of a second
- ③  $\frac{1}{80}^{\text{th}}$  of a second ✓
- ④  $\frac{1}{20}^{\text{th}}$  of a second



Q A stone of mass 1 kg is thrown with a velocity of 20 m/s across the frozen surface of a lake and it comes rest after travelling a distance of 50 m. What is the magnitude of the force opposing the motion of the stone.

$$\Delta p = m\vec{v}_f - m\vec{v}_i$$

$$= m(\vec{v}_f - \vec{v}_i)$$

$$= \frac{1}{20} [30 - (-20)]$$

$$= \frac{50}{20} = 2.5$$

$$\Delta t = \frac{\Delta p}{F_{\text{avg}}} = \frac{5}{2 \times 200} = \frac{1}{80}$$

Ans  $m = 1 \text{ kg}$   
 $v_i = 20 \text{ m/s}$



$f = \text{const} \leftarrow s = 50 \text{ m}$   
 $a = \text{const}$

or

$$s = \left( \frac{u+v}{2} \right) t$$

$$50 = \frac{20+0}{2} t$$

$$t = 5 \text{ sec}$$

$$F = \frac{\Delta p}{\Delta t} = \frac{0 - m u}{\Delta t}$$

$$= \frac{1 \times 20}{5} = 4 \text{ N}$$

2nd method

$$s = \frac{u^2}{2a}$$

$$v^2 - u^2 = 2as$$

$$a = \frac{20 \times 20}{2 \times 50} = 4$$

$$a = 4$$

$$f = ma$$

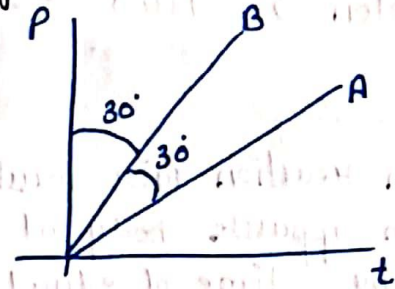
$$= 1 \times 4$$

$$f = 4 \text{ N}$$

B

Que For two object P-t graph is given then find Ratio of force acting on the

$$\frac{F_A}{F_B} = \frac{(\text{slope})_A}{(\text{slope})_B} = \frac{\tan 30}{\tan 60} = \frac{1}{3}$$



Que A force  $P = (2ti + 3t^2j) \text{ N}$  acts on object moving in xy plane. Find magnitude of change in momentum of the object in time interval  $t=0$  to  $t=2\text{ s}$ .

$$F = (2ti + 3t^2j)$$

$$F = \frac{dP}{dt}$$

$$dP = F \cdot dt$$

$$\int dP = \int 2t i dt + \int 3t^2 j dt$$

$$\Delta P = 2 \left( \frac{t^2}{2} \right)_0^2 i + 3 \left( \frac{t^3}{3} \right)_0^2 j$$

$$\Delta P = 4i + 8j$$

$$|\Delta P| = \sqrt{4^2 + 8^2}$$

$$= \sqrt{16 + 64}$$

$$= 8\sqrt{5}$$

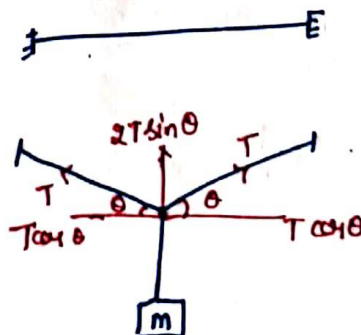
$$\boxed{4\sqrt{5} \text{ kg m/s}}$$

Que A force

- ① 7 sec
- ② 5 sec
- ③ 10 sec
- ④ 8 sec

Que A weight  $Mg$  is suspended from the middle of a rope whose ends are at the same level. The rope is no longer horizontal, the minimum tension required to completely straighten the rope is

- ①  $\frac{mg}{2}$
- ②  $mg \cos \theta$
- ③  $2mg \cos \theta$
- ④ Infinitely large



$$2T \sin \theta = mg$$

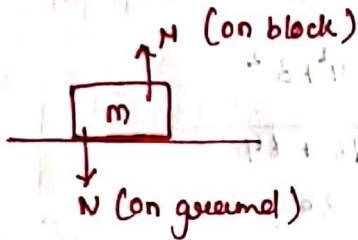
$$T = \frac{mg}{2 \sin \theta}$$

$$\boxed{T = \text{Infinitely large}} \quad R$$

Newton 3<sup>rd</sup> Law :- There is equal and opposite reaction for every action

# Action reaction pair must be on opposite body at a same time of equal magnitude but opposite in dire.

# Action reaction must be of same nature.



these two normal are (action - reaction pair)

### Significance of Newton's Law

① The first law talk about the natural state of motion of a body. i.e



Impulse  $\Rightarrow$  Impulse is defined as the change in momentum, It is measured as the product of the average force and time for which the force acts. It is a vector quantity directed along the direction of force.

$$F = \frac{dp}{dt}$$

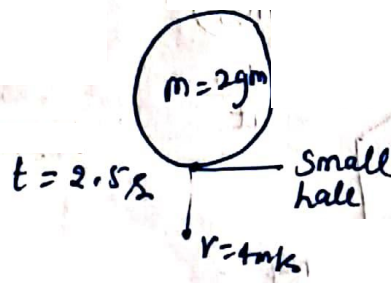
$$\int_{p_i}^{p_f} dp = \int F \cdot dt$$

$$p_f - p_i = \int F \cdot dt$$

$$\boxed{F = \int F \cdot dt}$$

Ques A balloon has 2g of air, a small hole is pierced into it. The air comes out with a velocity of 4 m/s. If the balloon shrinks completely in 2.5 s, the average force acting on the balloon is:

- ① 0.008 N
- ② 0.0032 N
- ③ 8 N
- ④ 3.2 N



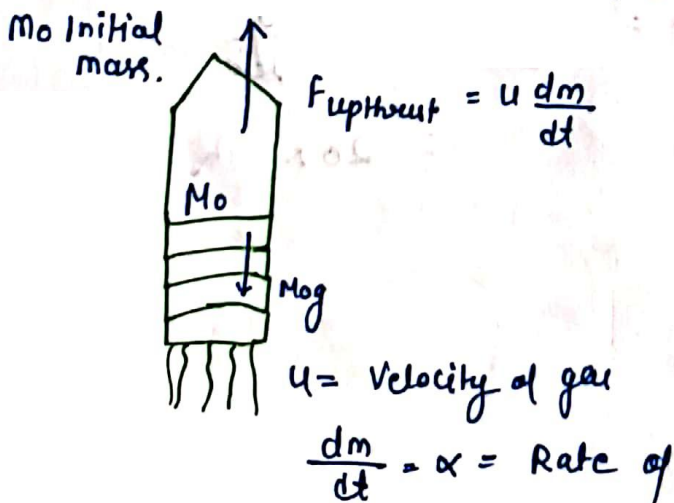
$$F_{\text{avg}} = u \frac{\Delta m}{\Delta t}$$

$$= 4 \times \frac{2}{1000 \times \frac{2.5}{2}}$$

$$= \frac{16 \times 3.2}{5 \times 1000}$$

$$\boxed{F = 0.0032 \text{ N}}$$

Rocket Problem  $\Rightarrow$  Variable mass system  $\frac{dm}{dt} \vec{v} = \text{const}$   
 $F = v \frac{dm}{dt}$



$$\text{Mass after time} = M_0 - \left( \frac{dm}{dt} t \right)$$

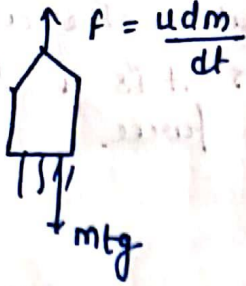
Initial accel<sup>n</sup>  $\Rightarrow$  F.B.D of Rocket ( $t=0$ )

$$F_{\text{net}} = u \frac{dm}{dt} - M_0 g$$

$$M_0 a_0 = u \frac{dm}{dt} - M_0 g$$

$$\boxed{a = \frac{u \frac{dm}{dt}}{M_0} - g}$$

after time  $t$



$$a_t = \frac{u \frac{dm}{dt}}{\left(m_0 - \frac{dm}{dt} t\right)} - g$$

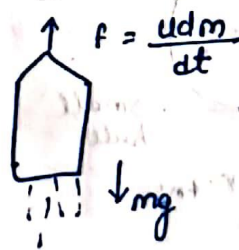
$$F_{net} = \frac{u dm}{dt} - m_t g$$

$$m_t a_t = \frac{u dm}{dt} - m_t g$$

$$a_t = \frac{\frac{u dm}{dt} - m_t g}{m_t}$$

Ques A 800 kg rocket fired from earth so that exhaust speed is 1200 m/s. then calculate mass of fuel burning per second, to provide initial thrust to overcome its weight ( $g = 10 \text{ m/s}^2$ )

$m = 800 \text{ kg}$   
 $u = 1200 \text{ m/s}$   
 $\frac{dm}{dt} = ?$



$$\frac{u dm}{dt} = mg$$

$$1200 \left(\frac{dm}{dt}\right) = 800 \times 10$$

$$\frac{dm}{dt} = \frac{80}{12} = 6.67 \text{ kg/s}$$

Ques A cracker rocket is ejecting gases at a rate of 0.05 kg/s with a velocity 400 m/s. The accelerating force of the rocket is ~~minute after the blast is ( $g = 10 \text{ m/s}^2$ )~~

- ~~1) 34.9 m/s<sup>2</sup>~~
- ~~2) 27.5 m/s<sup>2</sup>~~
- ~~3) 3.50 m/s<sup>2</sup>~~
- ~~4) 13.5 m/s<sup>2</sup>~~
- 1) 20 dyns
- 2) 20 N ✓
- 3) 200 N
- 4) zero

$$F = u \frac{dm}{dt} = 400 \times \frac{5}{100} = 20 \text{ N}$$

# Conservation of momentum

If net External force acting on the body / system is zero the momentum of body / system will be conserved.

$$\vec{F} = \frac{d\vec{p}}{dt}$$

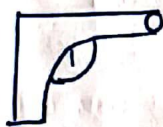
$$\text{If } \vec{F}_{\text{net}} = 0$$

$$0 = \frac{d\vec{p}}{dt}$$

$$\vec{p} = \text{Const}$$

$$\boxed{\vec{p}_f = \vec{p}_i}$$

Gun bullet System :-



System - Gun + bullet

M = mass of Gun

m = Mass of bullet

$$\vec{p}_i = 0$$

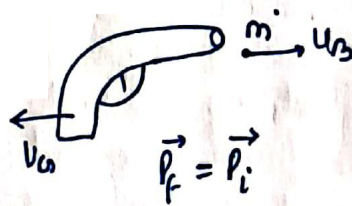
$$\boxed{(\vec{F}_{\text{ext}})_{\text{Gunbullet}} = 0}$$

$$K.E = \frac{p^2}{2m} \rightarrow \text{same}$$

$$R.E \propto \frac{1}{m}$$

$$\boxed{K.E_{\text{bullet}} > K.E_{\text{Gun}}}$$

$$\boxed{\frac{K.E_B}{K.E_G} = \frac{M}{m}}$$



$$m\vec{u}_B + M\vec{v}_G = 0$$

$$M\vec{v}_G = -m\vec{u}_B$$

$$\boxed{\vec{v}_G = -\frac{m\vec{u}_B}{M}}$$

$$\boxed{K.E = \frac{1}{2}mv^2 = \frac{p^2}{2m}}$$

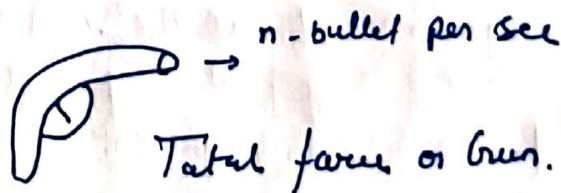
\* change in momentum of bullet =  $p_f - p_i = m\vec{u}_B$

\* Change in momentum of

$$\text{Gun} = m\vec{u}_B$$

$$= m\vec{u}_B$$

$$\boxed{\vec{p}_{\text{Gun}} = -\vec{p}_{\text{Bullet}}}$$



Total force on Gun.

$$\text{force on one bullet} = \frac{m\vec{u}_B}{t}$$

$$\text{force on n-bullet} = \frac{nm\vec{u}_B}{t}$$

$$\boxed{\text{force of n-bullet} = nm\vec{u}_B}$$

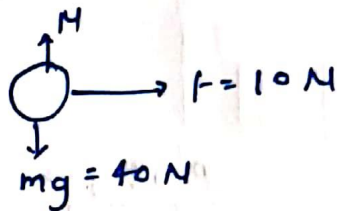
$$\text{force on Gun} = nm\vec{u}_B$$

# Dynamic of a body $\Rightarrow$

$$\vec{F}_{\text{net}} \text{ Unbalance time} = m\vec{a}$$



f.B.D of 4kg



$$N = 40 \text{ newton}$$

$$\Sigma f_x = 10 \text{ N}$$

$$ma = 10$$

$$4a = 10$$

$$a = \frac{10}{4} = \boxed{2.5 \text{ m/s}^2}$$



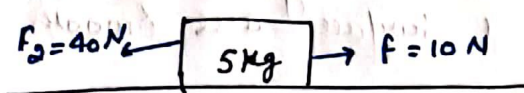
Find Acc<sup>n</sup> =

$$\Sigma f_x = (40 + 20)$$

$$10a = 60$$

$$\boxed{a = 6 \text{ m/s}^2}$$

Q<sub>4</sub>

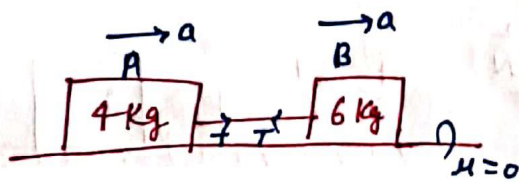


$$\Sigma f_x = m\vec{a}$$

$$30 = 5a$$

$$\boxed{a = 6 \text{ m/s}^2}$$

# Connected body motion :- Find accel<sup>n</sup> A & B and tension in string ?? Using equat<sup>n</sup> 1.



f.B.D of 4kg



$$T = 4a \text{ --- (1)}$$

f.B.D of 6kg



$$20 - T = 6a \text{ --- (2)}$$

$$20 - 4a = 6a$$

$$10a = 20 = \boxed{a = 2 \text{ m/s}^2}$$

$$T = 4a = 4 \times 2 = 8 \text{ m/s}^2$$

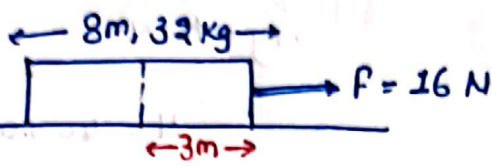


Ques A massive string of length 8m and mass 32 kg. Then find tension at a point 3m from an end where force is applied

$$a_{\text{body}} = \frac{F_{\text{net}}}{m}$$

$$= \frac{16}{32}$$

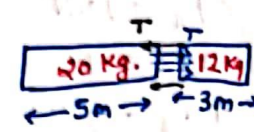
$$\vec{a} = \frac{1}{2} \text{ m/s}^2$$



MR

$$20 \text{ kg} \rightarrow a = \frac{1}{2}$$

$$T = 20 \times \frac{1}{2} = 10 \text{ N}$$



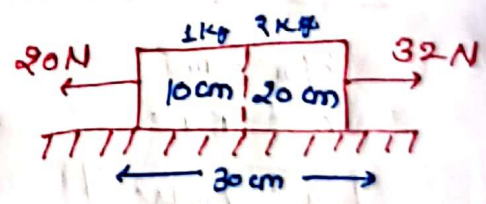
Mass of 8m is 32 kg  
 " " 1m =  $\frac{32}{8} = 4 \text{ kg/m}$   
 " " 3m =  $4 \times 3 = 12 \text{ kg}$ .

Ques Figure shows a uniform rod of length 30 cm having a mass 3.0 kg. The rod is pulled by constant forces of 20 N and 32 N as shown, find the force exerted by 20 cm part of the rod on the 10 cm part (all surfaces are smooth) is.

- ① 36 N
- ② 12 N
- ③ 54 N
- ④ 24 N

$$1 \text{ kg} = f = ma$$

$$1 \times 4 = 4$$



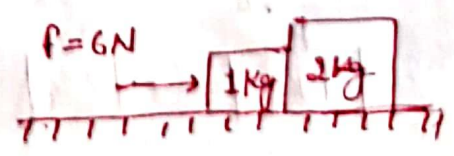
$$a = \frac{32 - 20}{3} = \frac{12}{3} = 4 \text{ m/s}^2$$

Ques Arrangement of two block system is as shown. The net force acting on 1 kg and 2 kg blocks are (assuming the surface to be frictionless) respectively.

- ① 4 N, 8 N
- ② 1 N, 2 N
- ③ 2 N, 4 N
- ④ 3 N, 6 N

$$a_{\text{sys}} = a_{1\text{kg}} = a_{2\text{kg}} = \frac{6 \text{ N}}{3}$$

$$a = 2 \text{ m/s}^2$$



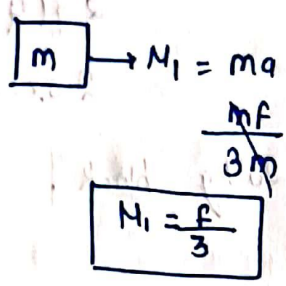
$$f_{2\text{kg}} = Ma = 1 \times 2 = 2 \text{ N}$$

$$f_{1\text{kg}} = ma = 2 \times 2 = 4 \text{ N}$$

Ques Two blocks are in contact on a frictionless table. One has mass  $m$  and the other  $2m$ . A force  $F$  is applied on  $2m$  as shown in the figure. Now the same force  $F$  is applied from right on  $m$ . In the two cases respectively, the ratio of force of contact b/w two blocks will be.

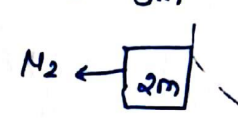
- ① Same  
 ② 1:2  
 ③ 2:1  
 ④ 1:3

Case-1  
 $a_{system} = \frac{F}{3m}$



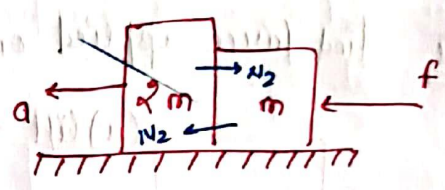
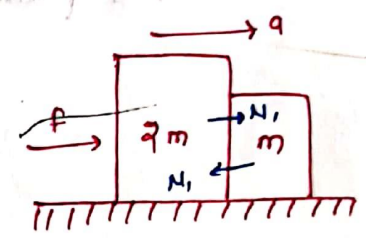
$N_1 = \frac{mF}{3m}$   
 $N_1 = \frac{F}{3}$

Case-2  
 $a_{sys} = \frac{F}{3m}$



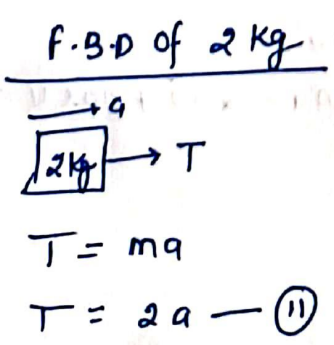
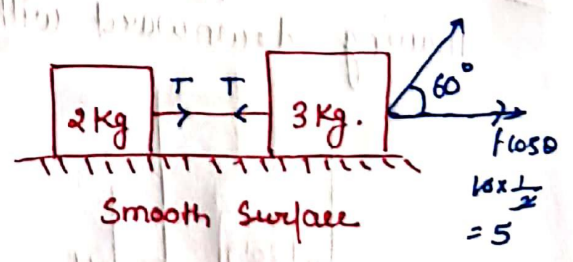
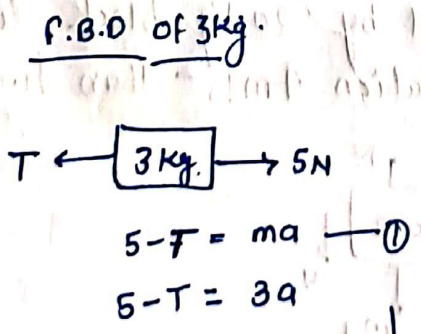
$N_2 = 2m \times \frac{F}{3m}$   
 $N_2 = \frac{2F}{3}$

$\Rightarrow \frac{N_1}{N_2} = \frac{1}{2}$  **B**



Ques Figure shows two blocks connected by a light inextensible string as shown in figure. A force of  $10N$  is applied on the bigger block at  $60^\circ$  with horizontal, then the tension in the string connecting the two masses is.

- ① 5N  
 ② 2N  
 ③ 1N  
 ④ 3N

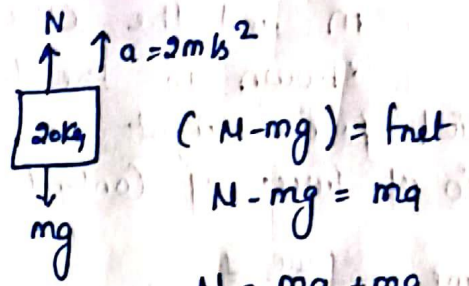
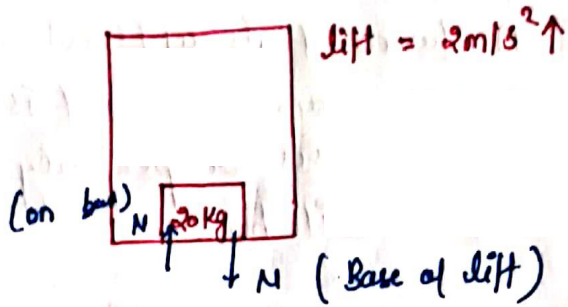


$5 - T = 3a$  — ①  
 $T = 2a$  — ②

---

$5 = 5a$   
 $a = 1 \text{ m/s}^2$   
 put the value of  $a$   $T = 2a$   
 $T = 2 \times 1 = 2 \text{ N}$  **B**

Ques Find force applied on base of lift by 20 kg block.



$$(N - mg) = ma$$

$$N - mg = ma$$

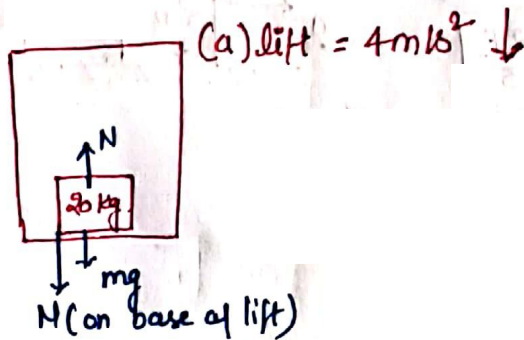
$$N = ma + mg$$

$$N = m(a + g)$$

$$20(2 + 10) = \boxed{240}$$

$$20 \times 12 = \boxed{240 \text{ N}}$$

Ques Find force applied on base of lift by 20 kg block.



$$N = 20(10 - 4)$$

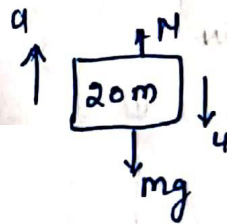
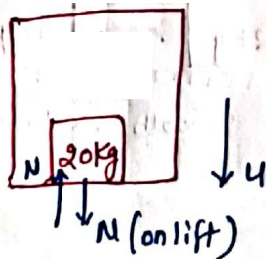
$$20 \times 6$$

$$= 120 \text{ N}$$

$$(mg - N) = ma$$

$$N = mg - ma = m(g - a)$$

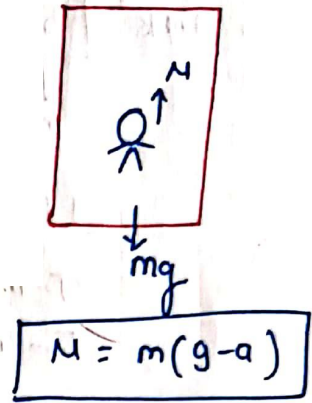
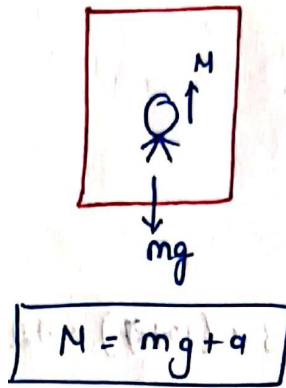
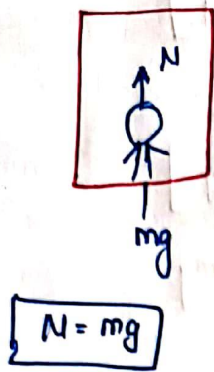
Ques Find force applied on base of lift by 20 kg block. lift is moving downward with acceleration  $4 \text{ m/s}^2$  then find Normal



$$N - mg = ma$$

$$N = mg + ma = 200 + 20 \times 4 = 280 \text{ N}$$

# Apparent Weight $\Rightarrow$

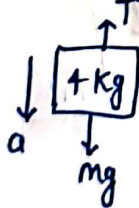


Ques Tension in the rope at the rigid support is ( $g = 10 \text{ m/s}^2$ )

- (a) 760 N
- (b) 1360 N
- (c) 1580 N
- (d) 1620 N

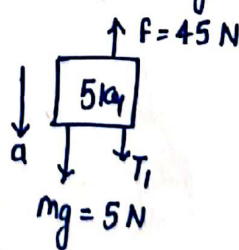
Ques Find tension in string b/w 4 kg and 5 kg

Sol<sup>n</sup> F.B.D of 4 kg



$$mg - T = 4 \times a \quad \text{--- (i)}$$

F.B.D of 5 kg



$$50 + T_1 = 45 = 5 \times a \quad \text{--- (ii)}$$



$$\text{(i) + (ii)}$$

$$50 + T - 45 = 5 \times 4 \quad \text{--- (iii)}$$

$$40 - T = 4a \quad \text{--- (iv)}$$

$$45 = 9a$$

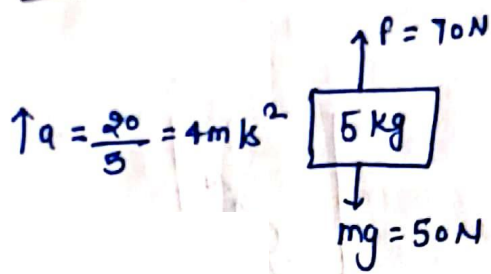
$$a = \frac{45}{9} = \boxed{5 \text{ m/s}^2}$$

Putting value of  $a$  in eq (i)

$$40 - T = 4 \times 5$$

$$T = 40 - 20 = \boxed{20 \text{ N}}$$

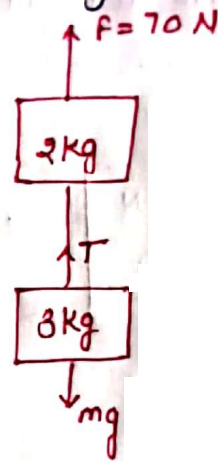
Ques Find tension in string connected b/w 2kg and 3kg.



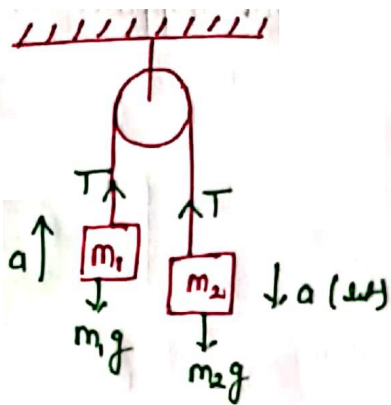
Think about

$$T - mg = ma$$

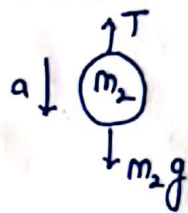
$$T = m(g + a) = 3 \times (10 + 4) = 42 \text{ N} \text{ Ans}$$



Ques If ( $m_2 > m_1$ ) then find acceleration of  $m_1$  and  $m_2$  and Tension in string.

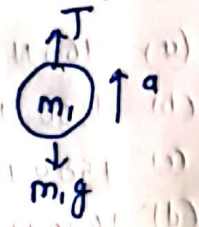


f.B.O of  $m_2$



$$m_2g - T = m_2a \quad \text{--- (i)}$$

f.B.O of  $m_1$



$$T - m_1g = m_1a \quad \text{--- (ii)}$$

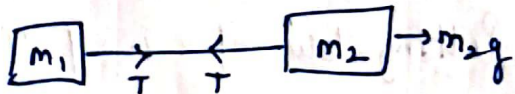
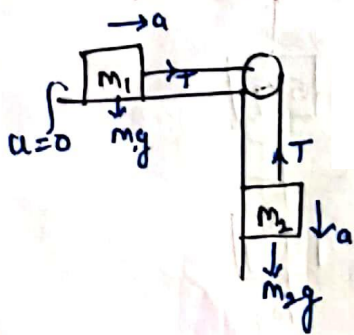
$$\textcircled{i} + \textcircled{ii} \quad m_2g - T = m_2a$$

$$T - m_1g = m_1a$$

$$\underline{m_2g - m_1g = (m_1 + m_2)a}$$

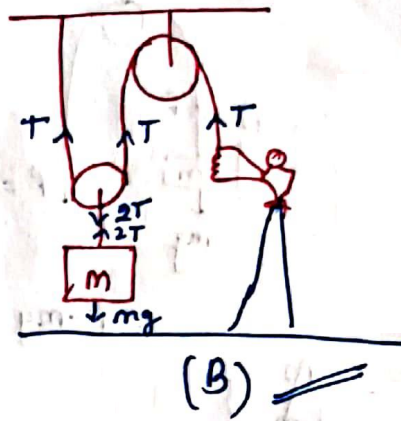
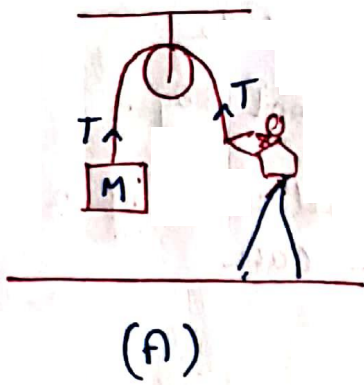
$$a = \frac{(m_2 - m_1)g}{m_2 + m_1} \text{ Ans}$$

Ques Find acceleration of block  $m_1$  and  $m_2$  and tension in string.



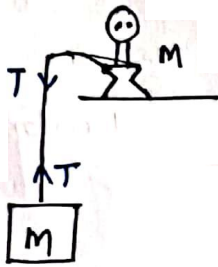
$$a = \left( \frac{m_2g}{m_1 + m_2} \right)$$

Ques In which case pulling the block will be easy

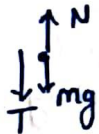


In case - B.

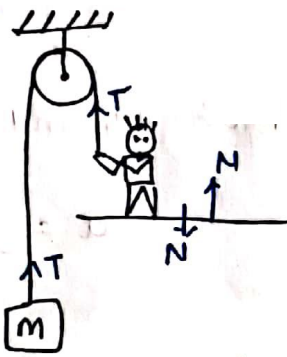
Ques



Man F.B.D



$$N = T + mg$$



Man F.B.D



In which case easy to pull.  
find Normal reaction of ground on man in both case

Ans B will be easy

$$T + N = mg$$

$$N = mg - T$$

Ques

The arrangement shown, the mass m will ascend with an acceleration (Pulley and rope are massless)

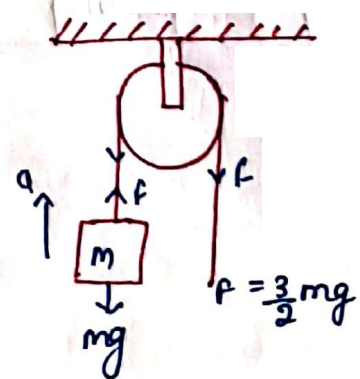
- ① zero
- ②  $\frac{g}{2}$  ✓
- ③ c
- ④  $2g$

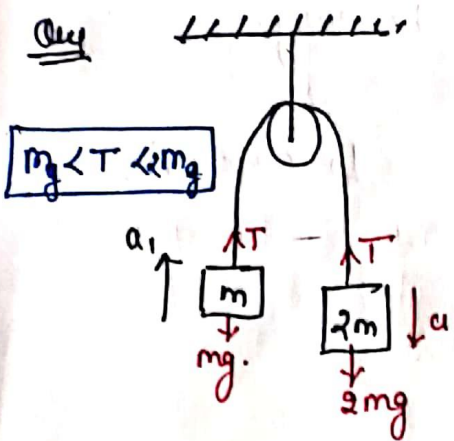
$$f - mg = ma$$

$$\frac{3}{2}mg - mg = ma$$

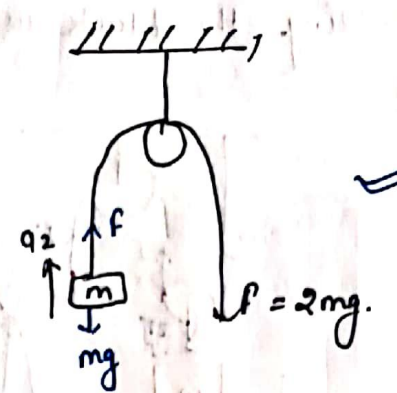
$$\frac{mg}{2} = ma$$

$$a = \frac{g}{2}$$





$$a = \left( \frac{2m - m}{2m + m} \right) g = \frac{m}{3m} g = \frac{g}{3}$$



$$F - mg = ma$$

$$2mg - mg = ma$$

$$mg = ma$$

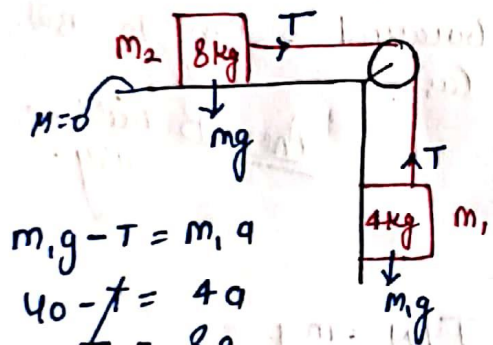
$$a_2 = g$$

- (a)  $a_1 = a_2$
- (b)  $a_1 > a_2$
- (c)  $a_1 < a_2$
- (d) Cont. Secy

find acceleration of m in Both Case.

Allen module case-3 Base.

Ques find acceleration of block  $m_1$  and  $m_2$  and tension in string.



$$m_1 g - T = m_1 a$$

$$40 - T = 4a$$

$$T = 8a$$


---


$$40 = 12a$$

$$a = \frac{40}{12} = \frac{10}{3} \text{ m/s}^2$$

$$a = \frac{m_1 g}{m_1 + m_2}$$

$$= \frac{40}{12} = \frac{10}{3}$$

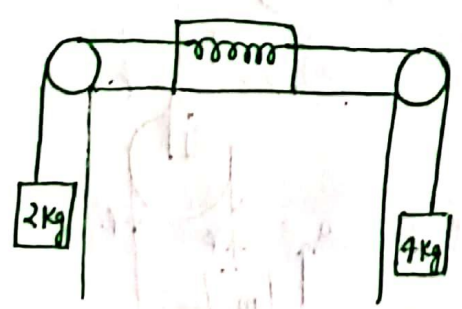
F.B.D of 8kg.

$$T = 8a$$

$$T = 8 \times \frac{10}{3} = \frac{80}{3}$$

$$T = \frac{m_1 m_2 g}{m_1 + m_2} = \frac{2 \times 4 \times 2}{4 + 2} g = \frac{8 \times 16g}{6} = \frac{8g}{3}$$

Ques Reading of spring.

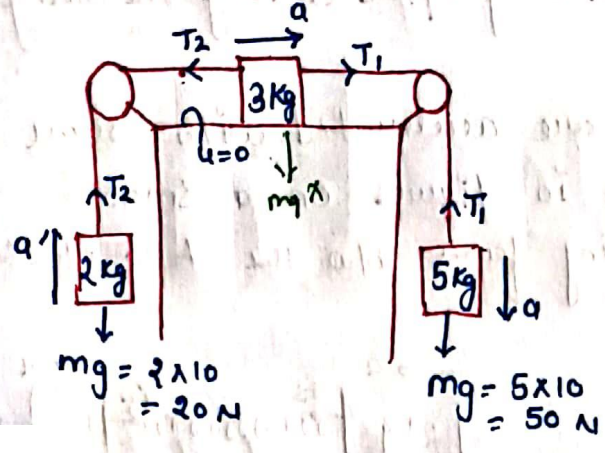


$$T = \frac{2 \times 4 \times 2}{4 + 2} g$$

$$= \frac{8 \times 16g}{6} = \frac{8g}{3}$$

II

Find accel<sup>n</sup> of system



f.B.D 5kg.

$$50 - T_1 = 5a \quad \text{--- (I)}$$

$$T_1 - T_2 = 3a \quad \text{--- (II)}$$

$$T_2 - 20 = 2a \quad \text{--- (III)}$$

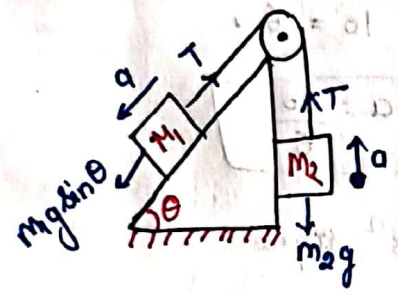

---


$$30 = 10a$$

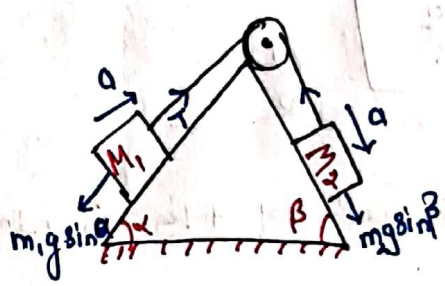
$$a = 3\text{ m/s}^2$$

Other module No Case 4, 5, 6.

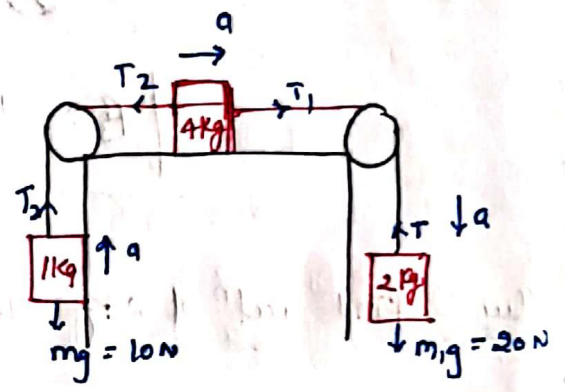
Ques Find acceleration of  $M_1$  and  $M_2$



$$a = \frac{m_1 g \sin \theta - m_2 g}{m_1 + m_2}$$



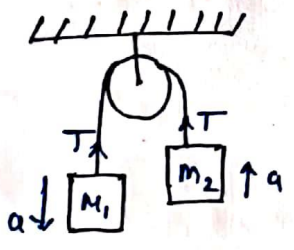
$$a = \frac{m_2 g \sin \beta - m_1 g \sin \alpha}{m_1 + m_2}$$



$$a = \frac{20 - 10}{7} = \frac{10}{7} \text{ m/s}^2$$

III  
Ques

Find Tension in string if  $(M_1 > M_2)$

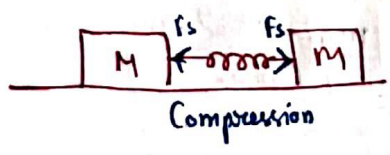
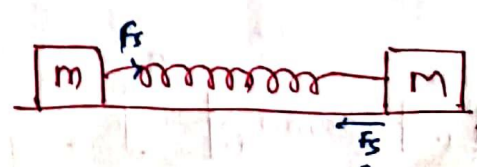
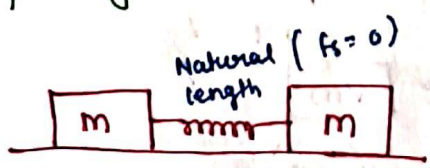


$$T = \frac{2m_1 m_2}{m_1 + m_2} g$$

$$T = \frac{2m_1 m_2}{m_1} g$$

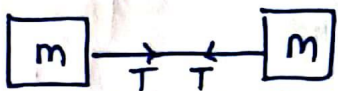
$$T = 2m_2 g$$

Spring force  $\rightarrow$



Spring force in spring becomes zero slowly after cutting the spring





Tension force in string becomes zero exactly after cutting the string.

Ques Two blocks of mass 2kg and 4kg are accelerated with same accel<sup>n</sup> by a force 10N as shown in figure on a smooth horizontal surface. then the spring force b/w the two blocks will be (Spring is massless)

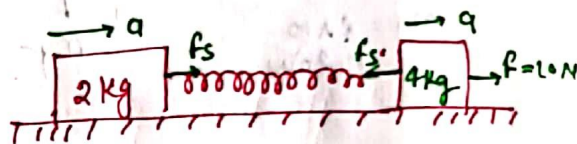
- Ⓐ 5N
- Ⓑ 10N
- Ⓒ  $\frac{10}{3}$  N
- Ⓓ  $\frac{5}{3}$  N

Using eqn - (1)

$$F_s = 2a$$

$$= 2 \times \frac{10}{3}$$

$$F_s = \frac{10}{3}$$



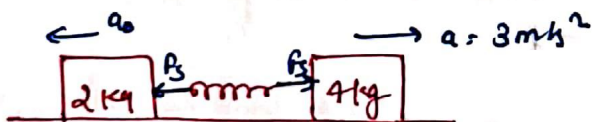
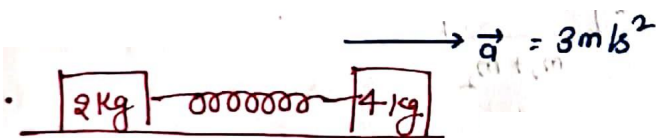
$$10 - \cancel{F_s} = 4a \quad \text{--- (1)}$$

$$\cancel{F_s} = 2a \quad \text{--- (2)}$$

$$10 = 6a$$

$$a = \frac{10}{6}$$

Ques Find accel<sup>n</sup> of 2kg if accel<sup>n</sup> of 4kg is  $3 \text{ m/s}^2$  right



$$F_s = 2 \times a_0$$

$$12 = 2a_0$$

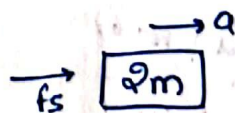
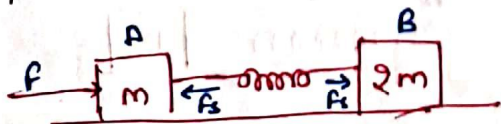
$$a_0 = \frac{12}{2} = 6 \text{ m/s}^2$$

$$F_s = m a$$

$$= 4 \times 3$$

$$= 12 \text{ N}$$

Ques Find accel<sup>n</sup> of B block if accel<sup>n</sup> of A block is  $a_0$  towards left



$$F_s = (2m) a'$$

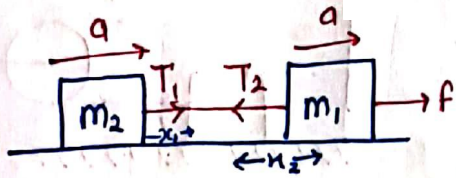
$$F + m a_0 = 2 m a'$$

$$a' = \frac{F + m a_0}{2m}$$

Sol<sup>n</sup>

$$F_s - F = m a_0 \quad \text{--- (1)}$$

Constraint Motion  $\Rightarrow$  Total work done by internal force is zero.

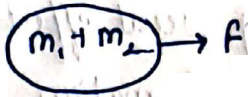


$T$  (internal force)

$$(W_{\text{tension}})_{\text{Total}} = 0$$

$$T_1 + T_2 \cos 180 = 0$$

$$W = T_1 x - T_2 x = 0$$



$$a = \left( \frac{F}{m_1 + m_2} \right)$$

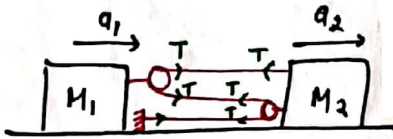
does not depend on tension.

Ques Constraint Motion  $\Rightarrow$  find relation b/w  $a_1$  and  $a_2$

Soln  $2x a_1 = 3x a_2$

$$2a_1 = 3a_2$$

Ans



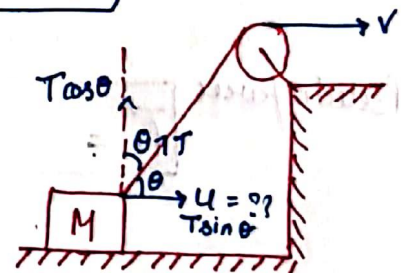
Ques A block is dragged on smooth plane with the help of a rope which moves with velocity  $v$ . The horizontal velocity of the block is.

$$T \cdot v = \text{const}$$

- ①  $v$
- ②  $\frac{v}{\sin \theta}$  ✓
- ③  $v \sin \theta$
- ④  $\frac{v}{\cos \theta}$

$$T \sin \theta u = T v$$

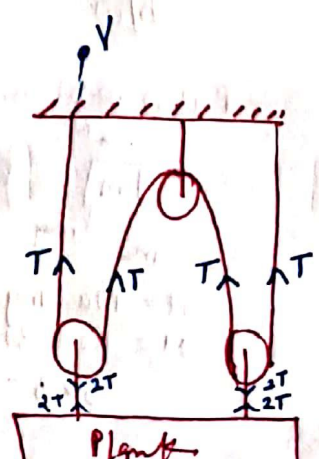
$$u = \frac{v}{\sin \theta}$$



HCV Ques And relation b/w  $a_1$  and  $a_2$

$$4T v_p = T v$$

$$v_p = \frac{v}{4}$$



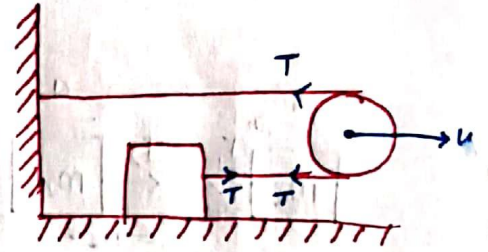
Qy In the figure shown, the pulley is moving with velocity  $u$ , the velocity of the block attached with string.

- ① 4u
- ② 3u
- ③ 4
- ④ 2u

$$2xu = v_0 T$$

$$v_0 = 2u$$

A1



Pseudo force  $\Rightarrow$  A Non real force having real effect  
 - Technique to Validate laws of motion in Non-Inertial frame of reference

<u>Pinki</u>	<u>Kallua</u>	<u>Ramlal</u>
rest ( $u=0$ )	$v = \text{const}$	$a \neq 0$
$\sum F_x = 0$	$\sum F_x = 0$	$\sum F_x = 0$
$a_x = 0$	$a_x = 0$	$a_x = a$
$\sum F_y = 0$	$\sum F_y = 0$	$\sum F_y = 0$
$a_y = 0$	$a_y = 0$	$a_y = 0$

- \* Law of motion Valid
- \* Inertia frame of reference
- \* Law of motion is not Valid
- \* Non inertial frame

Pseudo force  $\vec{F}_c = m\vec{a}$  only applicable in non-inertial accelerated frame

Ques Find Contact force b/w Block & Surface of lift.

F.B.D w.r.t Pinki

$$(N - mg) = ma$$

$$N = m(a + g)$$

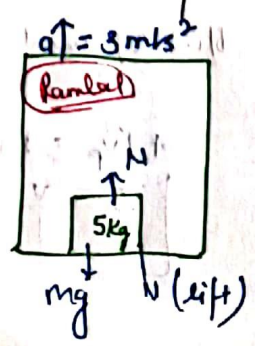
$$5(3 + 10) = 65$$

F.B.D w.r.t Ramlal

$$N = ma + mg$$

$$N = m(3 + 10)$$

$$5 \times 13 = 65 \text{ N}$$



Pinki

Ques A man weigh 80 kg. He stands on a weighing scale in a lift which is moving upwards with uniform acceleration of  $5 \text{ m/s}^2$ . What would be the reading on the scale ( $g = 10 \text{ m/s}^2$ )

- ① Zero
- ② 400 N
- ③ 800 N
- ④ 1200 N

$$N = m(g+a) \text{ or}$$

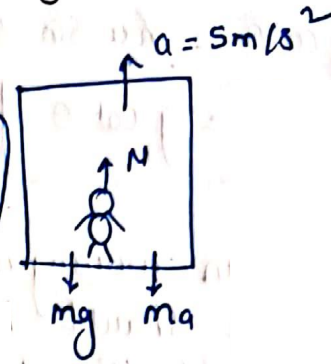
$$80(10+5)$$

$$80 \times 15$$

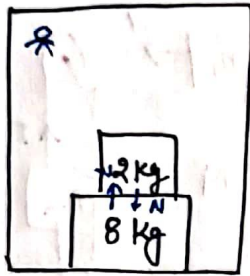
$$= 1200$$

$$N = mg + ma$$

$$m(g+a)$$



Ques



$a_{\text{lift}} = 4 \text{ m/s}^2$

find contact force b/w 2 kg & 8 kg

f.B.D of 2 kg w.r.t. lift



Rest w.r.t R.L

$$F_y = 0$$

$$N + ma = mg$$

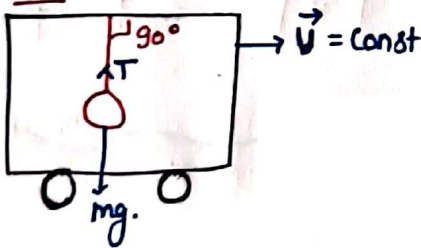
$$m(g+a)$$

$$2(10-4)$$

$$= 12 \text{ N}$$

Ques

CAR.

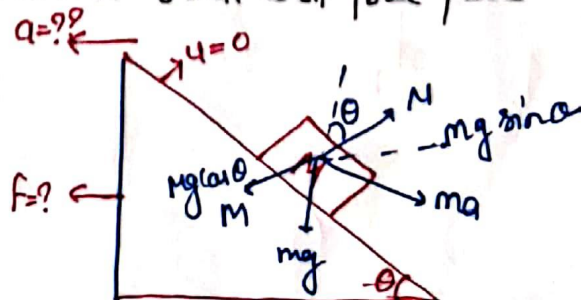


Ques Select the correct statement regarding pseudo force

1. It is electromagnetic in origin
2. Newton's 3rd Law is applicable for it.
3. It is a fundamental force
4. It is used to make Newton's law applicable in non-inertial frame

find accel<sup>n</sup> of inclined plane so that block will free fall

$$\text{free free fall} - N = 0$$



↳ to Incline

$$mg \cos \theta = N + ma \sin \theta$$

$$mg \cos \theta = ma \sin \theta$$

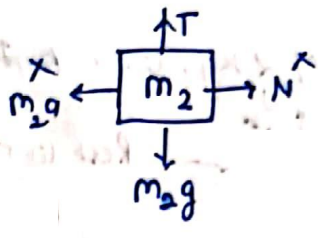
$$a = g \cot \theta$$

Ans

Ques In the given arrangement all surfaces are smooth, what acceleration should be given to the system, for which the block  $m_2$  doesn't slide down.

- ①  $\frac{m_2 g}{m_1}$
- ②  $\frac{m_1 g}{m_2}$
- ③  $g$
- ④  $\frac{m_2 g}{m_1 + m_2}$

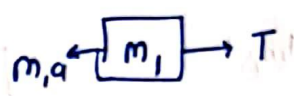
f.B.D of  $m_2$  w.r.t (R.L)



$\Sigma f_y = 0$

$$T = m_2 g \quad \text{--- (i)}$$

f.B.D of  $m_1$

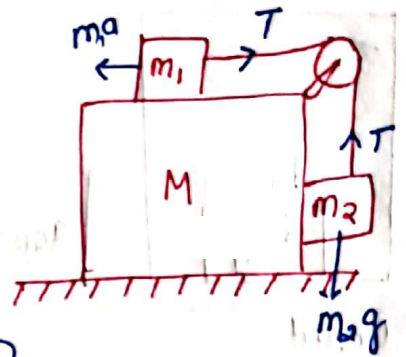


$\Sigma f_x = 0$

$$T = m_1 a \quad \text{--- (ii)}$$

① — ②

$$m_2 g = m_1 a$$



$$a = \frac{m_2 g}{m_1}$$